

## DE2.3 Electronics 2 for Design Engineers

### Tutorial Sheet 6 – Feedback Control (Lectures 16 - 19)

\* indicates level of difficulty

- 1.\* Reduce the figure given in Figure Q1 (a) to the standard feedback configuration illustrated in Figure Q1 (b). Express the transfer functions  $G$  and  $H$  in terms of  $G_1$ ,  $G_2$ ,  $H_1$  and  $H_2$

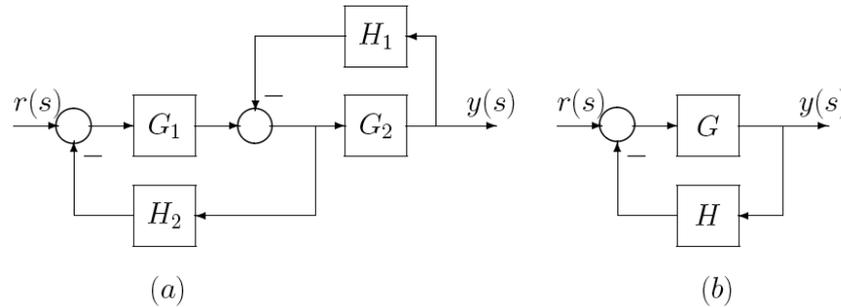


Figure Q1

2. A closed-loop system is used to track the sun to obtain maximum power from a photovoltaic panel. The tracking system is represented by the system shown in Figure Q2, where

$$G(s) = \frac{100}{\tau s + 1}$$

Assume that  $\tau = 3$  seconds nominally, calculate the time constant of the close-loop system response.

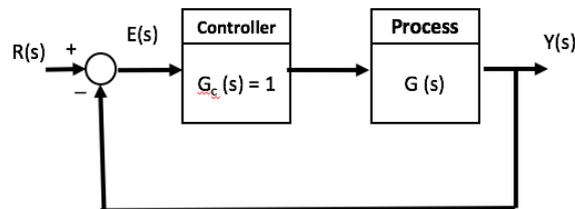


Figure Q2

- 3.\*\* Figure Q3 shows a first order system with a PI controller. The transfer functions of the plant  $P(s)$  and the controller  $C(s)$  are:

$$P(s) = \frac{b}{s + a} \quad \text{and} \quad C(s) = k_p + \frac{k_i}{s}$$

- (i) Derive loop transfer function of the system  $L(s)$ .
- (ii) Hence or otherwise, derive the transfer function of the closed loop system from reference  $r(t)$  to output  $y(t)$ .
- (iii) By rearranging the denominator of the transfer function in the form:

$$s^2 + 2\zeta\omega_0s + \omega_0^2,$$

derive expressions for  $k_p$  and  $k_i$  in terms of  $\zeta$ , the damping factor, and  $\omega_0$ , the natural or resonant frequency.

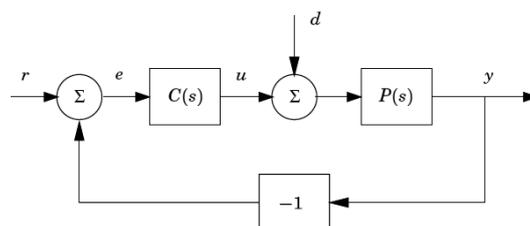


Figure Q3

- 4.\*\* Figure Q4 (a) shows an operational amplifier circuit - the amplifier gain is  $A(v_+ - v_-)$ . The input impedance is effectively infinite. The disturbance input  $v_n$  represents electrical noise. Determine the gains  $G_1$  and  $G_2$  from  $v_i$  to  $v_0$  (i.e. gain for input signal) and  $v_n$  to  $v_0$  (i.e. gain for disturbance), respectively. Show that the system is represented by block diagram Q2 (b).

The nominal values of the parameters are:  $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 100\Omega$  and  $A = 10^4$ .

- (i) Calculate  $G_1$  and  $G_2$  for these parameters. What conclusion can you make?
- (ii) Calculate separately the effects on  $G_1$  of a 10% change in  $R_1$ ,  $R_2$  and  $A$ .

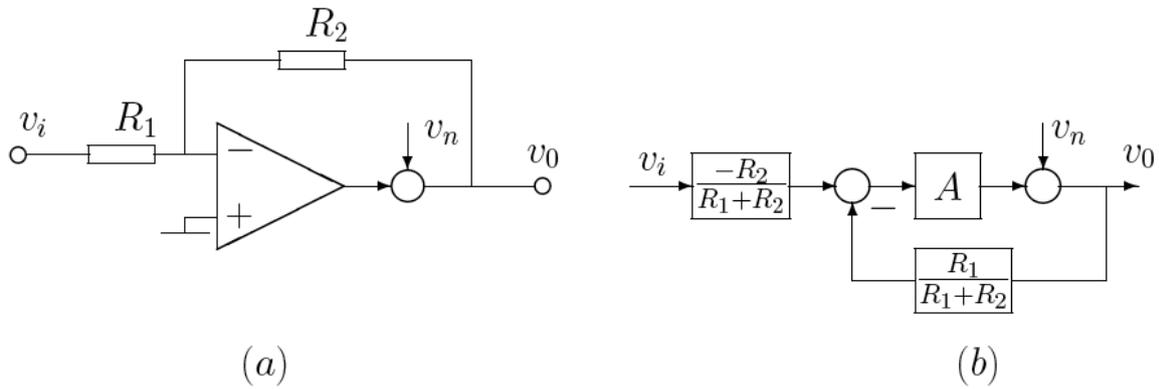


Figure Q4