

Parsing and Evaluation

Lecture 10

- The next two lectures cover parsing.
- To parse a sentence in a formal language is to break it down into its syntactic components.
- Parsing is one of the most basic functions every compiler carries out, as well as having many other uses.
- In this lecture, we'll be looking at how to define a formal language, and we'll study an example of parsing and evaluating an arithmetic expression.

Backus-Naur Form

- Parsing is an operation that's carried out on *formally defined* languages. So how do we formally define a language?
- We do it using another formally defined language, called a *meta-language*, such as **Backus-Naur** Form (or BNF).
- Here's an example of BNF. It defines what a “product” is.

$$\langle \text{product} \rangle ::= \langle \text{number} \rangle \mid \langle \text{product} \rangle * \langle \text{number} \rangle$$

- This says that a product is either a number or a number followed by “*” followed by another product. Note that it's a recursive definition.
- The “|” symbol is part of BNF, and it means “or”. (The “*” symbol is not part of BNF, but is part of the language being defined.)

Arithmetic Expressions in BNF

- The following BNF definitions describe the syntax of an arithmetic expression.

```
<expression> ::=      <term> |  
                        <expression> + <term> |  
                        <expression> - <term>  
  
<term>      ::=      <factor> |  
                        <term> * <factor> |  
                        <term> / <factor>  
  
<factor>    ::=      <number> | ( <expression> )
```

Examples of Arithmetic Expressions

- From the preceding definitions, it should be clear that the following are all syntactically correct expressions:

5

5 + 8

(5 + 8)

5 * 2 + 1

5 * (2 + 1)

- while the following are not:

+

5 +

((5 + 8)

5 * 2 + + 1

Lexical Analysis I

- Before we parse a sentence in a formal language, it's convenient to break it down into a list of lexemes.
- A **lexeme** (sometimes also called **token**) is the smallest syntactic unit in a language. The following are typical kinds of lexemes:
 - Numbers (ie: numeric strings)
 - Names (ie alphanumeric strings)
 - Operators (including brackets) (eg: *, +, ^, etc)
- For example, the sentence “(64 + 7) * 128” is broken down into a list of seven lexemes: “(”, “64”, “+”, “7”, “)” , “*”, and “128”.

Lexical Analysis II

- In what follows, we'll assume that the expression is a string pointed to by a pointer "expression".
- We'll also assume we have the following access functions already written:

```
bool notEmpty (const string& expression);  
//returns true if expression is not empty string  
  
char nextChar (const string& expression);  
//returns next character in expression, nothing consumed  
  
char getNextChar (string& expression);  
//returns next character in expression, char consumed  
  
int getNum (string& expression);  
//returns value of next integer in expression, consume integer
```

- Don't worry about the data type string and how these access functions are written for now. We will deal with them later.

Recursive versus Iterative Processing

- Here's the BNF for an expression again.

$$\begin{aligned}\langle \text{expression} \rangle ::= & \langle \text{term} \rangle \mid \\ & \langle \text{expression} \rangle + \langle \text{term} \rangle \mid \\ & \langle \text{expression} \rangle - \langle \text{term} \rangle\end{aligned}$$

- This definition is **left-recursive** — the recursive part is the leftmost item on the right-hand-side on the definition. If we translated this directly into a recursive procedure, it would go into an infinite loop.
- Here's a **right-recursive** version which defines the same thing.

$$\begin{aligned}\langle \text{expression} \rangle ::= & \langle \text{term} \rangle \mid \\ & \langle \text{term} \rangle + \langle \text{expression} \rangle \mid \\ & \langle \text{term} \rangle - \langle \text{expression} \rangle\end{aligned}$$

- The right-recursive version can be translated directly into a recursive parsing procedure, but processes expressions in the reverse order to what we require.
- So we use the left-recursive version, and translate it into an **iterative procedure**.

Evaluating an Expression I

- Here's the BNF again.

```
<expression> ::=      <term> |  
                        <expression> + <term> |  
                        <expression> – <term>
```

- To **evaluate** an expression E iteratively, this is what you do.
 - Evaluate the next term in E, and call the result X.
 - While the next character in E is an operator (“+” or “–”),
 - Read past the operator.
 - Evaluate the next term in E, calling the result Y.
 - Let X be $X + Y$ or $X - Y$, depending on the operator.
- The value of E is the final value of X.

Evaluating an Expression II

- Here's the C++ code. It should be self-explanatory.

```
void evalExpression (string& expression, int& result) {
    int temp;
    char op;

    evalTerm (expression, result);
    while ((notEmpty(expression)) &&
           ((nextChar(expression)=='+' ||
            nextChar(expression)=='-'))){
        op = getNextChar(expression);
        evalTerm(expression, temp);
        if (op=='+')
            result = result + temp;
        else
            result = result - temp;
    }
}
```

Evaluating a Term I

- Evaluating a term is almost identical. Here's the BNF.

$$\begin{aligned} \langle \text{term} \rangle ::= & \quad \langle \text{factor} \rangle \mid \\ & \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \\ & \langle \text{term} \rangle / \langle \text{factor} \rangle \end{aligned}$$

- To evaluate a term T, this is what you do.
 - Evaluate the next factor in T, and call the result X.
 - While the next character in T is an operator (“*” or “/”),
 - Read past the operator.
 - Evaluate the next factor in T, calling the result Y.
 - Let X be $X * Y$ or X / Y , depending on the operator.
- The value of T is the final value of X.

Evaluating a Term II

- And here's the C++ code.

```
void evalTerm (string& expression, int& result) {
    int temp;
    char op;

    evalFactor (expression, result);
    while ((notEmpty(expression)) &&
           ((nextChar(expression) == '*' ) ||
            (nextChar(expression) == '/' ))) {
        op = getNextChar(expression);
        evalFactor(expression, temp);
        if (op == '*')
            result = result * temp;
        else
            result = result / temp;
    }
}
```

Evaluating a Factor I

- Evaluating a factor is a little different, and involves a recursive call. Here's the BNF again.

$$\langle \text{factor} \rangle ::= \langle \text{number} \rangle \mid (\langle \text{expression} \rangle)$$

- To evaluate a factor F , this is what you do.
 - If the next character in F isn't "(" then let X be the first number in F .
 - Otherwise evaluate the next expression in F , and call the result X . Then read past the ")".
- The value of F is X .

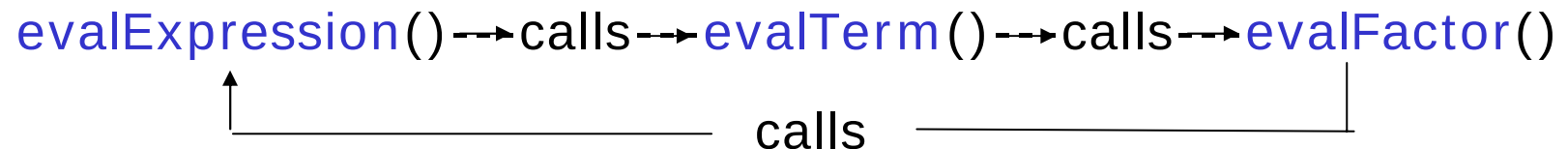
Evaluating a Factor II

- Here's the C++ code.

```
void evalFactor (string& expression, int& result) {  
  
    if (notEmpty(expression) &&  
        (nextChar(expression) != '('))  
        result = getNum(expression);  
    else {  
        getNextChar(expression);           // skip '('  
        evalExpression(expression, result);  
        getNextChar(expression);           // skip ')'  
    }  
}
```

Evaluating a Factor III

- Note that `evalExpression()`, `evalTerm()` and `evalFactor()` are **mutually recursive**. That is:



- We need to use function prototype to specify functions arguments before they are used. Here are the function prototype for all three functions:

```
void evalExpression (string& expression, int& result);  
void evalTerm (string& expression, int& result);  
void evalFactor (string& expression, int& result);
```

Access Routines I - strings

- Borland C++ understand a data type called **string**. Here are some examples of access functions for string data type. (They are actually membership functions, something we will consider in a later lecture.)

```
string s1;  
string s2 = "initial value";  
s3.insert (3, "123");           // s3 = "ini123tial value"  
s3.erase (4, 2);               // s3 = "ini3tial value"  
s3.replace (4, 2, "pqr");      // s3 = "intpqrrial value"  
  
char d[16];  
strcpy(d, s3.c_str());         // copy s3 into array d  
cout << s3.length() << endl;  // returns no of char in s3  
s1 = "mississippi";  
cout << s1.find("ss") << endl; // returns 2  
cout << s1.find("ss", 3) << endl; // returns 5  
if (s2.empty())  
    cout << "string is empty" << endl;
```

Access Routines II

- Now we can write our access routines for this program:

```
//----- Access Routines -----  
  
bool isNum (char c) {  
    //returns true if c is 0-9  
    return ((c >= '0') && (c <= '9'));  
}  
  
bool notEmpty (const string& expression) {  
    //returns true if expression is not empty string  
    return (!expression.empty());  
}  
  
char nextChar (const string& expression) {  
    //returns next character in expression, nothing consumed  
    return expression[0];  
}
```

Access Routines III

```
char getNextChar (string& expression) {  
    //returns next character in expression, char consumed  
    char c = '\\0';  
    if (notEmpty(expression)) {  
        c = expression[0];  
        expression.erase(0,1);    //eat one character  
    }  
    return c;  
}
```

Access Routines IV

```
int getNum (string& expression) {  
    //returns value of next integer in expression, consume integer  
    string numToken;  
    int i=0;  
    int maxString = expression.length();  
    while (isNum(expression[i]) && i<=maxString)  
        i++;  
    numToken = expression.substr(0, i);    //extract the number string  
    expression = expression.erase(0, i);  //remove it from expression  
    return atoi(numToken.c_str());        //convert string to integer  
}  
// End of Access Routines
```

Example

expression → 7 * (5 + 4)

```
void evalExpression (string& expression, int& result) {  
    int temp;  
    char op;  
  
    evalTerm (expression, result);  
    while ((notEmpty(expression)) &&  
           ((nextChar(expression)=='+' ||  
            nextChar(expression)=='-'))){  
        op = getNextChar(expression);  
        evalTerm(expression, temp);  
        if (op=='+')  
            result = result + temp;  
        else  
            result = result - temp;  
    }  
}
```

Example

expression → 7 * (5 + 4)

```
void evalExpression (string& expression, int& result) {  
    void evalTerm (string& expression, int& result) {  
        int temp;  
        char op;  
  
        evalFactor (expression, result);  
        while ((notEmpty(expression)) &&  
                ((nextChar(expression)=='*') ||  
                 (nextChar(expression)=='/'))){  
            op = getNextChar(expression);  
            evalFactor(expression, temp);  
            if (op=='*')  
                result = result * temp;  
            else  
                result = result / temp;  
        }  
    }  
}
```

Example

expression

→ 7 * (5 + 4)

Returns result = 7
expression string = " *(5+4)"

```
void evalExpression (string& expression, int& result) {
```

```
void evalTerm (string& expression, int& result) {
```

```
void evalFactor (string& expression, int& result) {
```

```
    if (notEmpty(expression) &&  
        (nextChar(expression) != '('))
```

```
        result = getNum(expression);
```

```
    else {
```

```
        getNextChar(expression);           // skip '('
```

```
        evalExpression(expression, result);
```

```
        getNextChar(expression);           // skip ')'
```

```
    }
```

```
}
```

Example

op = *

expression

(5 + 4)

result = 7

```
void evalExpression (string& expression, int& result) {  
    void evalTerm (string& expression, int& result) {  
        int temp;  
        char op;  
  
        evalFactor (expression, result);  
        while ((notEmpty(expression)) &&  
            ((nextChar(expression) == '*' ) ||  
             (nextChar(expression) == '/' ))) {  
            op = getNextChar(expression);  
            evalFactor(expression, temp);  
            if (op == '*')  
                result = result * temp;  
            else  
                result = result / temp;  
        }  
    }  
}
```

Example

expression

5 + 4)

nextChar() = (

```
void evalExpression (string& expression, int& result) {
```

```
void evalTerm (string& expression, int& result) {
```

```
void evalFactor (string& expression, int& result) {
```

```
    if (notEmpty(expression) &&  
        (nextChar(expression) != '('))
```

```
        result = getNum(expression);
```

```
    else {
```

```
        getNextChar(expression);           // skip '('
```

```
        evalExpression(expression, result);
```

```
        getNextChar(expression);           // skip ')'
```

```
    }
```

```
}
```

Example

expression

5 + 4)

nextChar() = (

```
void evalExpression (string& expression, int& result) {
```

```
void evalTerm (string& expression, int& result) {
```

```
void evalFactor (string& expression, int& result) {
```

```
void evalExpression (string& expression, int& result) {
```

```
int temp;
```

```
char op;
```

```
evalTerm (expression, result);
```

```
while ((notEmpty(expression)) &&  
      ((nextChar(expression)=='+' ||  
        nextChar(expression)=='-'))){
```

```
    op = getNextChar(expression);
```

```
    evalTerm(expression, temp);
```

```
    if (op=='+')
```

```
        result = result + temp;
```

```
    else
```

```
        result = result - temp;
```

```
}
```

```
}
```

Example

expression

5 + 4)

Result = 5

```
void evalExpression (string& expression, int& result) {
```

```
void evalTerm (string& expression, int& result) {
```

```
void evalFactor (string& expression, int& result) {
```

```
void evalExpression (string& expression, int& result) {
```

```
void evalTerm (string& expression, int& result) {
```

```
int temp;
```

```
char op;
```

```
evalFactor (expression, result);
```

```
while ((notEmpty(expression)) &&  
      ((nextChar(expression) == '*' ||  
       nextChar(expression) == '/'))){
```

```
    op = getNextChar(expression);
```

```
    evalFactor(expression, temp);
```

```
    if (op == '*')
```

```
        result = result * temp;
```

```
    else
```

```
        result = result / temp;
```

```
}
```

```
}
```

Example

op = +

expression

+ 4)

Returns temp = 4

```
void evalExpression (string& expression, int& result) {  
    void evalTerm (string& expression, int& result) {  
        void evalFactor (string& expression, int& result) {  
            void evalExpression (string& expression, int& result) {  
                int temp;  
                char op;  
  
                evalTerm (expression, result)  
                while ((notEmpty(expression)) &&  
                    ((nextChar(expression) == '+' ||  
                     nextChar(expression) == '-')) {  
                    op = getNextChar(expression);  
                    evalTerm(expression, temp);  
                    if (op == '+')  
                        result = result + temp;  
                    else  
                        result = result - temp;  
                }  
            }  
        }  
    }  
}
```

result = 9

Example

expression →)

result = 9

```
void evalExpression (string& expression, int& result) {  
    void evalTerm (string& expression, int& result) {  
        void evalFactor (string& expression, int& result) {  
            if (notEmpty(expression) &&  
                (nextChar(expression) != '('))  
                result = getNum(expression);  
            else {  
                getNextChar(expression);           // skip '('  
                evalExpression(expression, result);  
                getNextChar(expression);           // skip ')'  
            }  
        }  
    }  
}
```

Example

expression →

result = 7

temp = 9

```
void evalExpression (string& expression, int& result) {  
    void evalTerm (string& expression, int& result) {  
        int temp;  
        char op;  
  
        evalFactor (expression, result)  
        while ((notEmpty(expression)) &&  
            ((nextChar(expression) == '*' ||  
              nextChar(expression) == '/'))){  
            op = getNextChar(expression);  
            evalFactor(expression, temp);  
            if (op == '*')  
                result = result * temp;  
            else  
                result = result / temp;  
        }  
    }  
}
```

Example

expression →

final result = 63

```
void evalExpression (string& expression, int& result) {  
    int temp;  
    char op;  
  
    evalTerm (expression, result);  
    while ((notEmpty(expression)) &&  
           ((nextChar(expression) == '+' ||  
            nextChar(expression) == '-'))){  
        op = getNextChar(expression);  
        evalTerm(expression, temp);  
        if (op == '+')  
            result = result + temp;  
        else  
            result = result - temp;  
    }  
}
```